

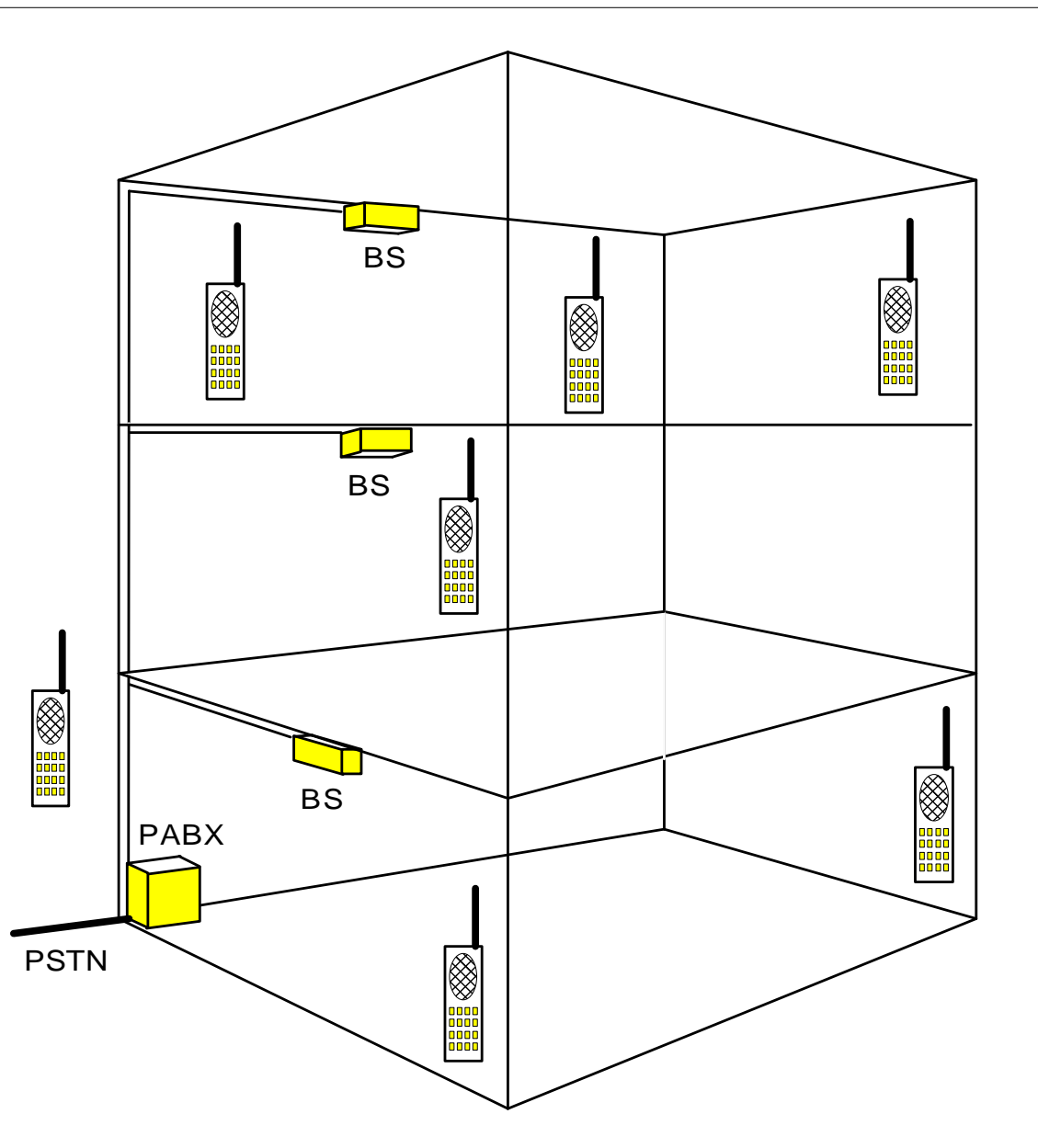
# Optimal Planning of Digital Cordless Telecommunication Systems <sup>a</sup>

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<sup>a</sup>Work was done at ECRC, Munich, Germany



Using a Mobile  
Phone in a  
Building

## The POPULAR prototype

Data :

- A blue-print of the building
- Information about the materials used for walls and ceilings

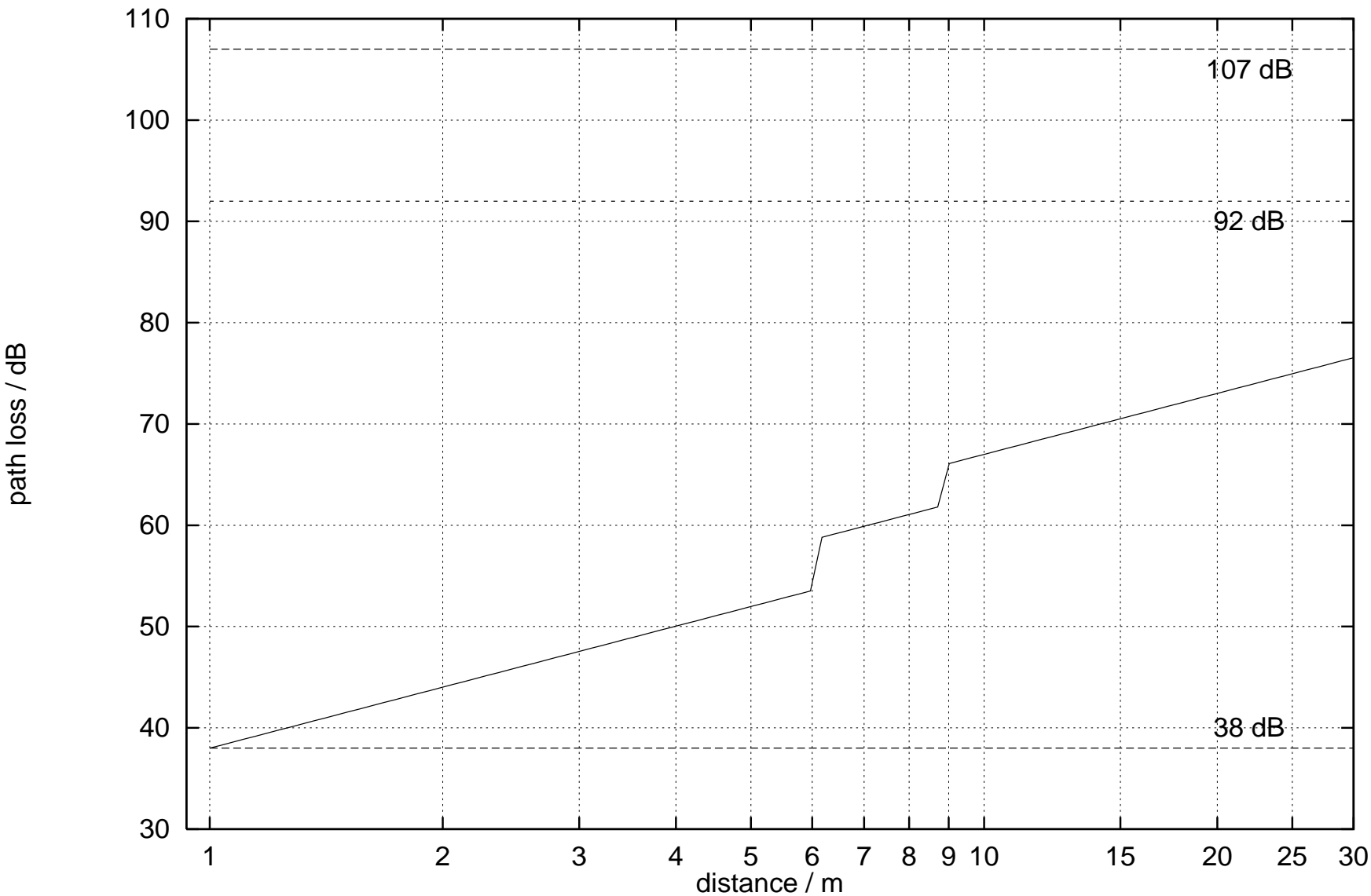
The problem :

- Placing senders to cover all the rooms in the building
- Computing the minimum number of senders needed

The solution :

- Using constraint technology

# Propagation model: loss/distance



**Propagation model (cont.)**

$$L = L_{1m} + 10n \log_{10} d + \sum_i k_i F_i + \sum_j p_j W_j$$

$L$  Total path loss in  $dB$

$L_{1m}$  path loss in  $1m$  distance from the sender

$n$  propagation factor

$d$  distance between transmitter and receiver

$k_i$  number of floors of kind  $i$  in the propagation path

$F_i$  attenuation factor of one floor of kind  $i$

$p_j$  number of walls of kind  $j$  in the propagation path

$W_j$  attenuation factor of one wall of kind  $j$

## Direct Encoding

A naive solution would be to

- Discretize the space in grid points  $P_i$
- Express the relation (constraint) between senders  $S_j$  positions and signal level at each point  $P_i$  :  
$$\text{Signal}(P_i) = \max_j (\text{Signal}(S_j) - \text{Loss}(S_j, P_i))$$
- Express that the signal must be above a threshold at each point :  
$$\text{Signal}(P_i) \geq \text{Threshold}$$

It does not work because the relations are too complex to constrain senders positions.

## Dual Problem

Since the propagation of a signal is not directional, sender and receiver can be exchanged.

Therefore the two following properties are equivalent :

Each grid point is reached by the signal of one sender :

$$\forall P_i \exists S_j \quad P_i \in \text{Covered}(S_j)$$

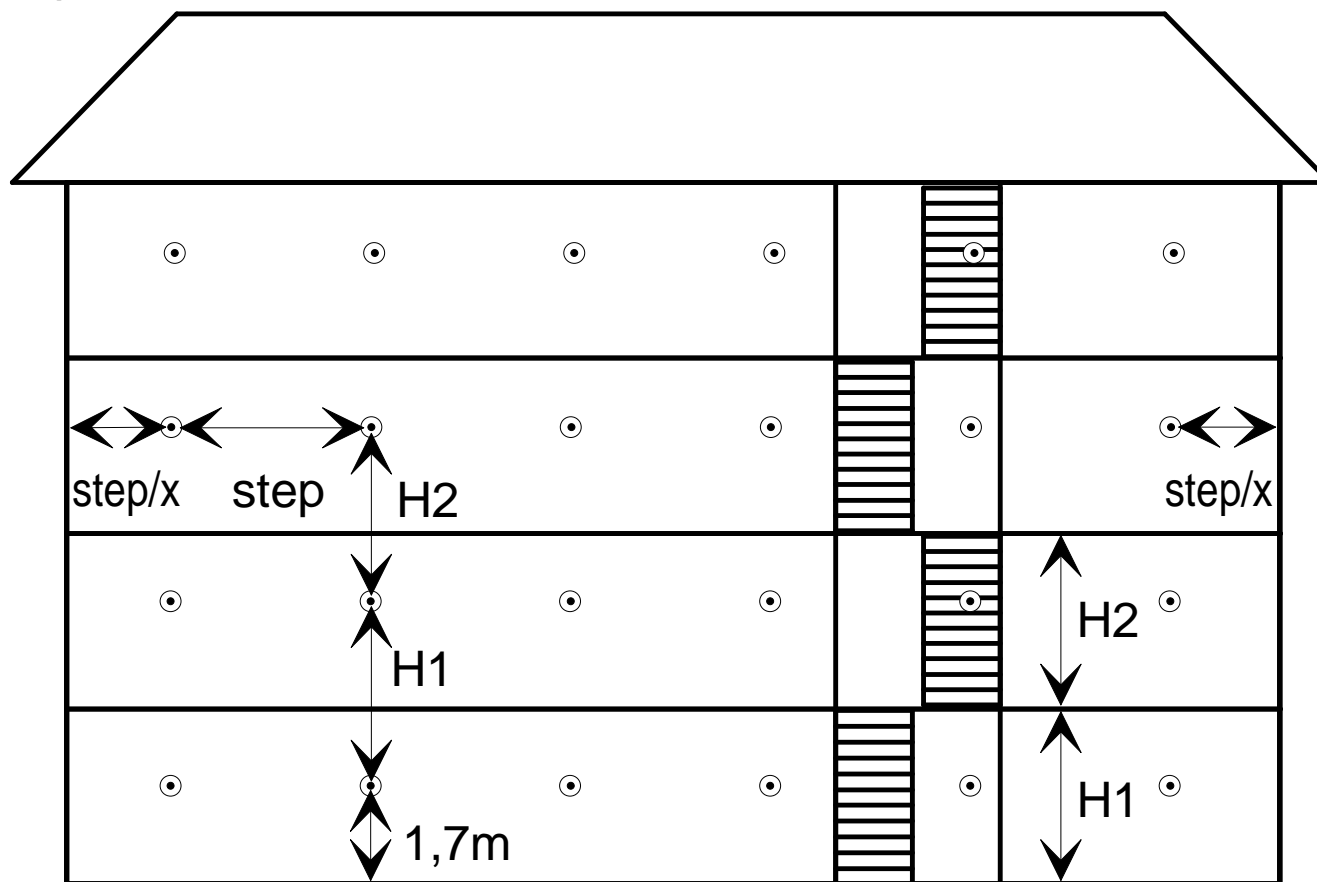
There is a sender in the neighbourhood of each grid point :

$$\forall P_i \exists S_j \quad S_j \in \text{Covered}(P_i)$$

The dual problem is easier to solve because the  $\text{Covered}(P_i)$  zones can be statically computed.

# Grid of test points

⊙ test point





## Representation of Covered Surfaces

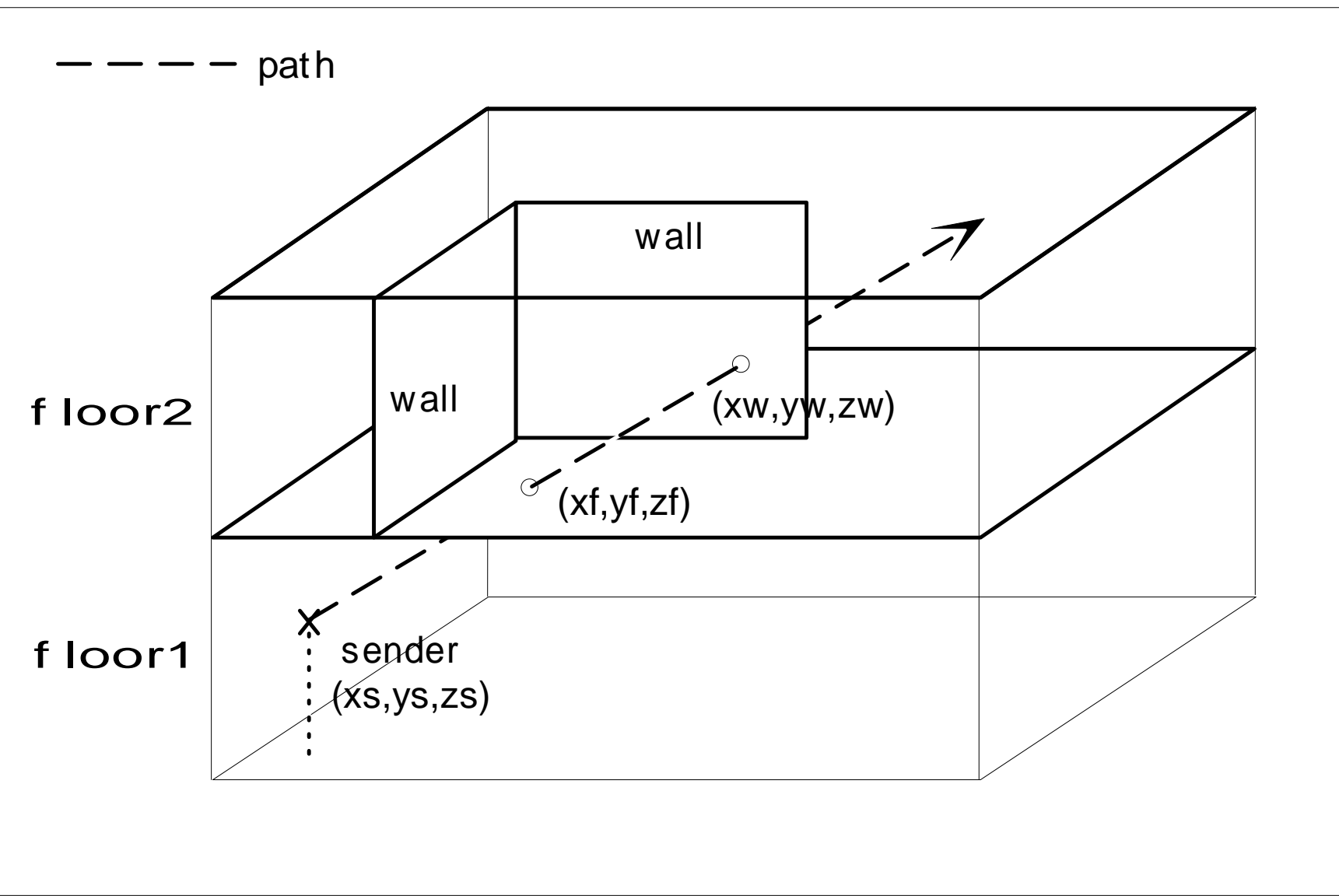
In order to express the constraint  $S_j \in Covered(P_i)$ , the  $Covered(P_i)$  must be simple enough. It can be approximated by

- A rectangle
- A list of rectangles

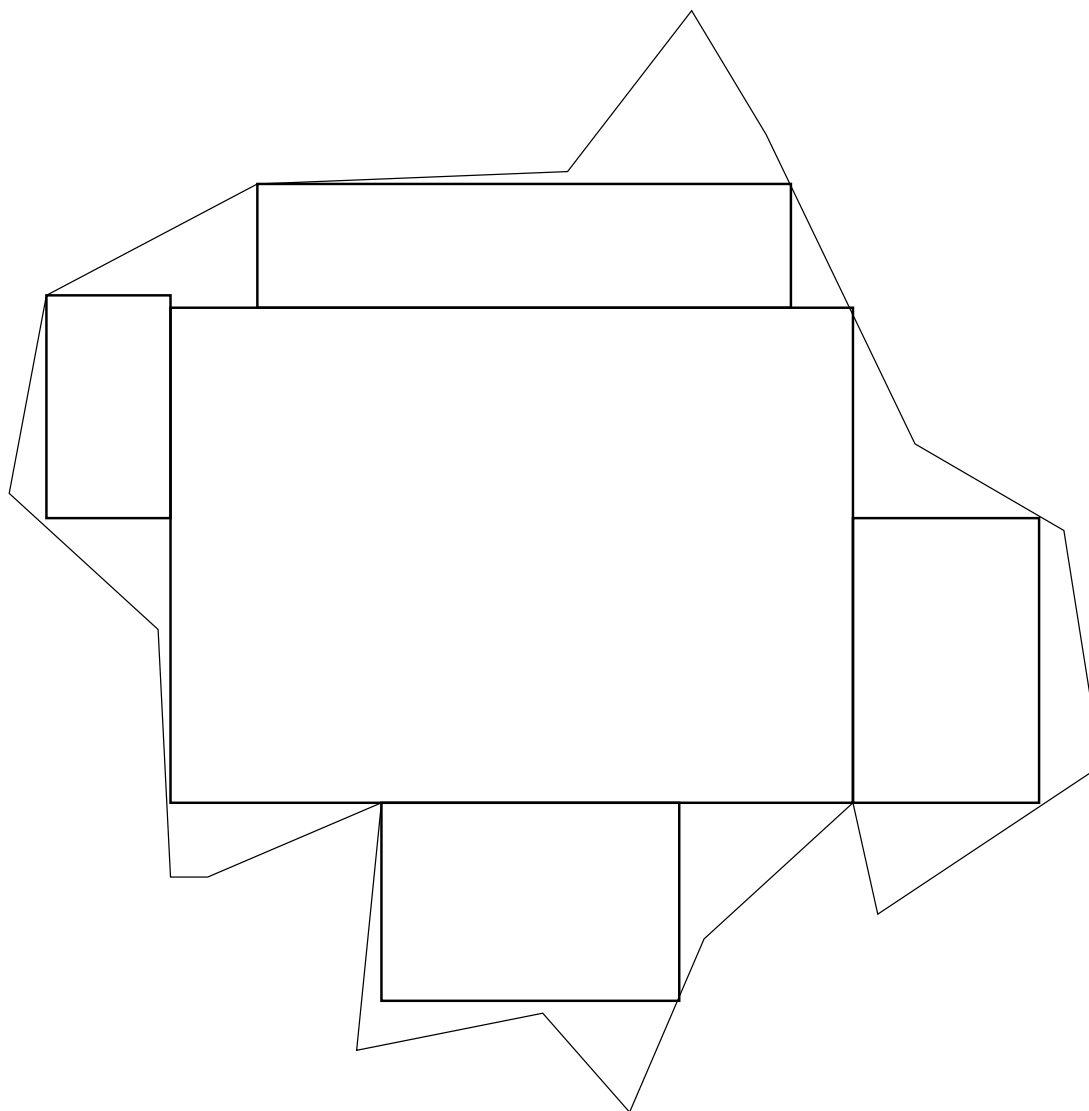
### Algorithm

1. Compute the  $Covered(P_i)$  zone by ray tracing for each  $P_i$
2. Approximate  $Covered(P_i)$
3. Set the constraints  $S_j \in Covered(P_i)$
4. Do clever labeling

# Ray Tracing



## Approximation by a Union of Rectangles



## Constraint Handling Rules

**What?** : A declarative language designed for writing user-defined constraints : a committed-choice language with multi-headed rules for rewriting the constraints into simple ones.

**How ?** : A library for the Prolog ECL<sup>i</sup>PS<sup>e</sup> system including

- a translator from constraint handling rules to Prolog code,
- a runtime for handling the constraint store.

## CHR inside constraint

Rules for the **inside** constraint stating that a point is **inside** a rectangle

```
% inside((X0, Y0), (XLeftLow, YLeftLow)-(XRightUp, YRightUp))
```

```
inside(_, (Xm, Ym)-(XM, YM)) ==>
```

```
  Xm < XM, Ym < YM.
```

```
inside((X, Y), (Xm, Ym)-(XM, YM)) ==>
```

```
  Xm < X, X < XM, Ym < Y, Y < YM.
```

```
inside(XY, (Xm1,Ym1)-(XM1,YM1)), inside(XY, (Xm2,Ym2)-(XM2,YM2)) <=>
```

```
  Xm is max(Xm1,Xm2), Ym is max(Ym1,Ym2),
```

```
  XM is min(XM1,XM2), YM is min(YM1,YM2),
```

```
  inside(XY, (Xm,Ym)-(XM,YM)).
```

## Extension to Union of Rectangles

Rules for the `inside` constraint stating that a point is within a list of rectangles (a GEOMETRICAL object)

$$\text{inside}(S, L1), \text{inside}(S, L2) \Leftrightarrow$$
$$\text{intersect\_geoms}(L1, L2, L3),$$
$$\text{inside}(S, L3).$$
$$\text{intersect\_geoms}(L1, L2, L3) \Leftrightarrow$$
$$\text{setof}(\text{Rect}, \text{intersect\_geom}(L1, L2, \text{Rect}), L3).$$
$$\text{intersect\_geom}(L1, L2, \text{Rect}) \Leftrightarrow$$
$$\text{member}(\text{Rect1}, L1), \text{member}(\text{Rect2}, L2),$$
$$\text{intersect\_rectangles}(\text{Rect1}, \text{Rect2}, \text{Rect}).$$

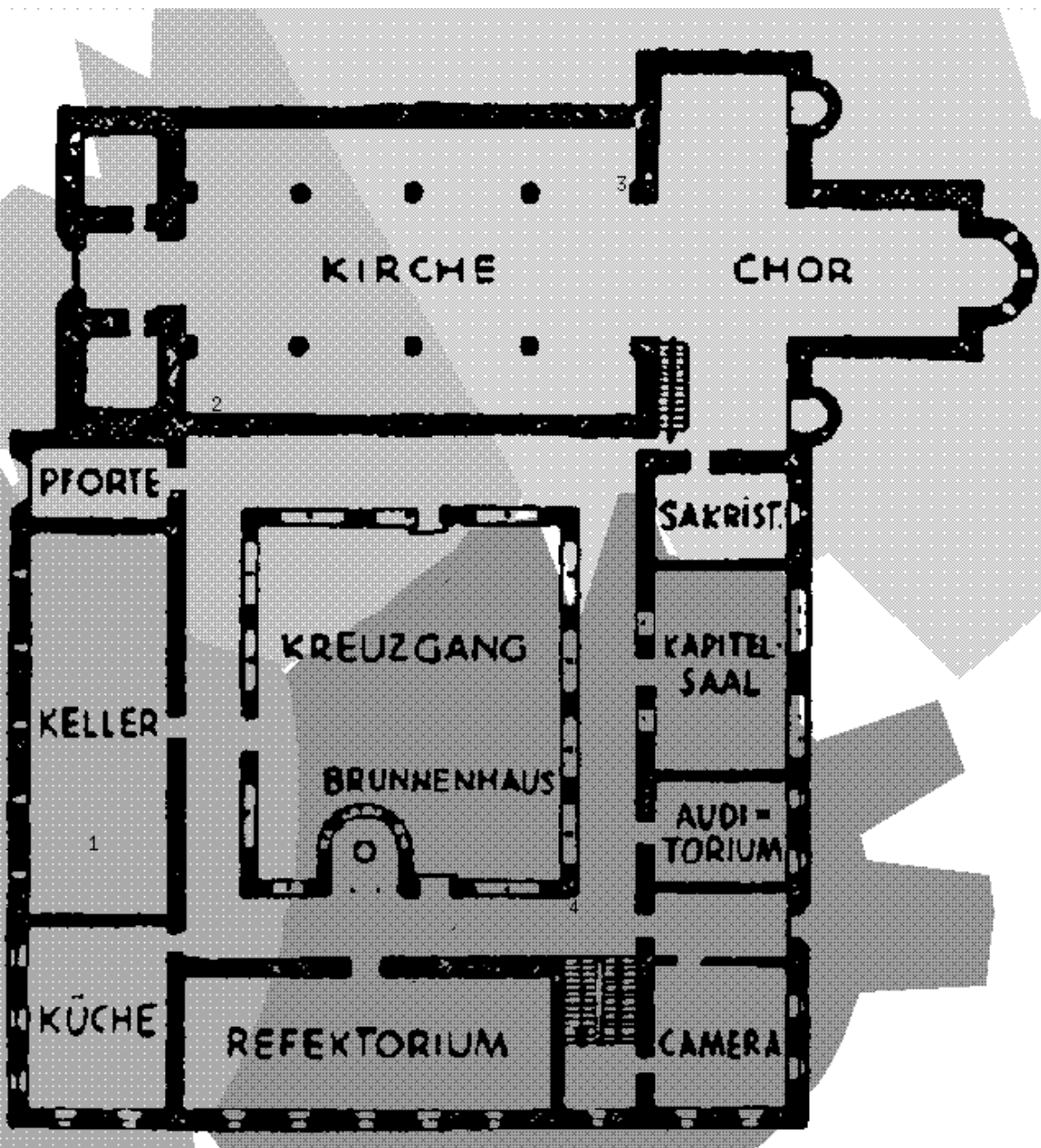
## Labeling

The constraint phase associates a sender to each  $Covered(P_i)$  zone. The labeling phase has to choose the number and the positions of the senders. It is expressed by stating that as many senders as possible are equal.

```
equate_senders([]) <=> true.
```

```
equate_senders([S|L]) <=>
```

```
( member(S, L) or true ), % Try to equate a sender with others  
equate_senders(L).
```



A True Example



## Conclusion

On this application, constraint technology (CHR) proves to

- have big expression power: the whole program for solving the problem is only a couple of hundred lines and required few man-months to be implemented.
- be flexible: the first prototype was easily extended from rectangles to union of rectangles, from 2-D to 3-D, ...
- be extensible: for example, restricting allowed senders locations to walls needs only one more inside constraint.
- be efficient: for a typical office building, an optimal placement is found within a few minutes (up to 25 base stations).